



Central Questions

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We think we know the answers to all of these questions ...

... but no one has been able to prove that even a small part of this "world-view" is correct.

If we're wrong on any one of these then computer science will change dramatically

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Introduction

- · You already know about two complexity classes - P = the set of problems decidable in *polynomial time* - NP = the set of problems with witnesses that can be checked in polynomial time ... and notion of NP-completeness
- Useful tool
- Deep mathematical problem: P = NP? Course should be both useful and mathematically interesting

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 $f: \Sigma^* \to \Sigma^*$ · function problem: given x, compute f(x) • decision problem: $f: \sum^* \rightarrow \{yes, no\}$ given x, accept or reject CS151 Lecture 1 16

Problems and Languages

· simplification doesn't give up much:

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- Given an integer n, find its prime factors - Given an integer n and an integer k, is there a factor of n that is < k?

- Given a Boolean formula, find a satisfying assignment - Given a Boolean formula, is it satisfiable?

- can solve function problem efficiently using related decision problem (how?)
- · We will work mostly with decision problems

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